

$$t \rightarrow \infty: J_{31}(t), J_{23}(t), J_{12}(t) \rightarrow J_{\text{const.}}$$

stationary state current

$$J = \frac{k_1 k_2 k_3}{D} \left(1 - \frac{r_1 r_2 r_3}{k_1 k_2 k_3} \right)$$

↳ func. of rates > 0

$$\frac{k_1}{r_1} = e^{-\beta(H_3 - H_1 - \mu_{\text{ATP}})}$$

$$\frac{k_2}{r_2} = e^{-\beta(H_2 - H_3)} \quad E_{\text{in}} \text{ for photon}$$

$$\frac{k_3}{r_3} = e^{-\beta(H_1 - H_2 + \mu_{\text{ADP}} + \mu_{\text{P}} + E_{\text{out}})}$$

E_{out} for photon

$$\Rightarrow J = \frac{k_1 k_2 k_3}{D} \left(1 - e^{-\beta(\underbrace{\mu_{\text{ATP}} - \mu_{\text{ADP}} - \mu_{\text{P}} - E_{\text{out}}}_{\equiv \Delta\mu})} \right)$$

$$\mu_{\text{ATP}} = \mu_{\text{ATP},0} + k_B T \ln C_{\text{ATP}}$$

↑
conc. of ATP in sol'n

chemical pot. diff. for ATP hydrolysis reaction = diff. in chem. pots. of inputs - outputs of reaction

$$\mu_{\text{ADP}} = \mu_{\text{ADP},0} + k_B T \ln C_{\text{ADP}}$$

$$\mu_{\text{P}} = \dots$$

$$\Rightarrow \Delta\mu = \overbrace{\mu_{\text{ATP},0} - \mu_{\text{ADP},0} - \mu_{\text{P},0}}^{12 k_B T} + k_B T \ln \frac{C_{\text{ATP}}}{C_{\text{ADP}} C_{\text{P}}}$$

$\Delta\mu \approx 21-29 k_B T$ for modern cells across all life

if $E_{out} < \Delta\mu \Rightarrow J > 0$ NESS

power budget:

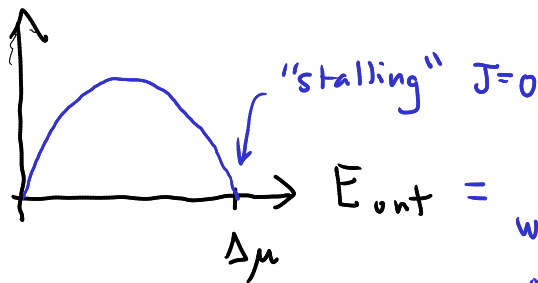
$$\dot{W}_{\text{net power in}} = \frac{1}{2} \sum_{nm} J_{nm} W_{nm}$$
$$\stackrel{t \rightarrow \infty}{=} J (\Delta\mu - E_{out})$$
$$= P_{in} - P_{out}$$

where $P_{in} = J \Delta\mu$ $P_{out} = J E_{out}$

efficiency: $\eta = \frac{P_{out}}{P_{in}} = \frac{E_{out}}{\Delta\mu}$

$$P_{out} = J(E_{out}) E_{out}$$

typically $\approx 0.4 - 0.6$ for motor proteins



E_{out} = amount of work you put on the motor ("load")

