

ordinary
LDB

$$\Rightarrow \frac{\Omega_{nm}}{\Omega_{mn}} = e^{-\beta(E_n - E_m)}$$

(sys.
exchanging therm.
energy w/ env.
at temp T)

$$\Rightarrow ESS \quad p_n^s = \frac{e^{-\beta E_n}}{Z}$$

$$\Downarrow$$

$$J_{nm}^s = 0$$

To get NESS we need to modify LDB:

end result: $\frac{\Omega_{nm}}{\Omega_{mn}} = e^{-\beta(E_n - E_m - \underbrace{W_{nm}}_{\text{"work" done on sys. during } m \rightarrow n \text{ trans.}})}$

conservative work

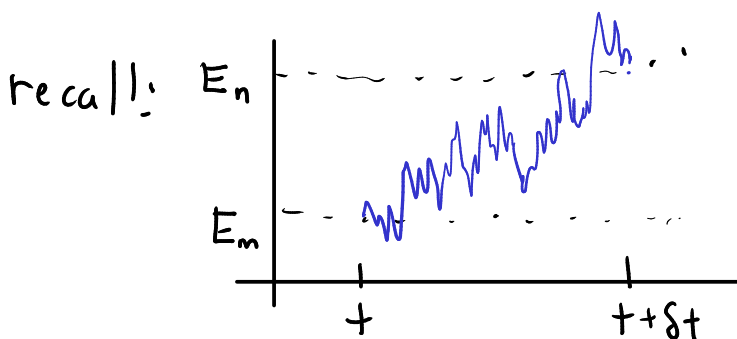
$$W = \int \vec{F} \cdot d\vec{x} = U_{\text{end}} - U_{\text{start}}$$

$$\vec{F} = -\nabla U$$

where $W_{nm} \neq \Phi_n - \Phi_m$
for any func. Φ_n

work has to be non-conservative
(at least in part)

How to get this extra term?



$\Omega_{nm} \delta t \propto$ prob. that
env. takes us from
 $E_m \rightarrow E_n$ in time δt
(donates $E_n - E_m$ in energy)

$$\Rightarrow \frac{\Omega_{nm}}{\Omega_{mn}} = e^{-\beta Q_{nm}} \quad \text{here: } Q_{nm} = E_n - E_m$$

how much
ther. energy we need
from env. during
 $m \rightarrow n$ trans
 $\equiv$ "heat"

$\beta = \frac{1}{k_B T}$

imagine we have "help" from another energy source, in which case:

$$Q_{nm} = E_n - E_m - \underbrace{W_{nm}}$$

"work":

energy from
another (non-therm.)
source

$W_{nm} > 0$: help
work into sys.

during
 $m \rightarrow n$
trans.

$W_{nm} < 0$: hurt
work output from sys.

$W_{nm} = 0$: transition
does not couple to
any other energy
source

general LDB:

$$\frac{\Omega_{nm}}{\Omega_{mn}} = e^{-\beta Q_{nm}} = e^{-\beta (E_n - E_m - W_{nm})}$$